

3. Un péndulo consiste en una masa m conectada a una cuerda de longitud L . La masa se desplaza de modo que la cuerda forma un ángulo de θ_0 con la vertical, y luego se libera la masa describe un semicírculo. Encuentre la expresión para la velocidad y la tensión de la cuerda cuando la masa pasa por la parte inferior.

$$\begin{aligned} W_{\text{Ext}} &= 0 \\ \oint W_{\text{NC}} &= \int \vec{T} \cdot d\vec{l} \\ d\vec{l} &= \vec{\omega} dt \end{aligned}$$

$$\begin{aligned} h_1 &= h \\ v_1 &= 0 \end{aligned}$$

$$\begin{aligned} v_2 &=? \\ h_2 &= 0 \end{aligned}$$

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$

$$\begin{aligned} \vec{T} &= T \hat{j} \\ \vec{G} &= G \hat{i} \\ \vec{A} \cdot \vec{G} &= T \cdot G = 0 \end{aligned}$$

$$W_{\text{NC}} = 0$$



$$\Delta E_{\text{mec}} = 0$$

$$E_{\text{mec},1} = E_{\text{mec},2}$$

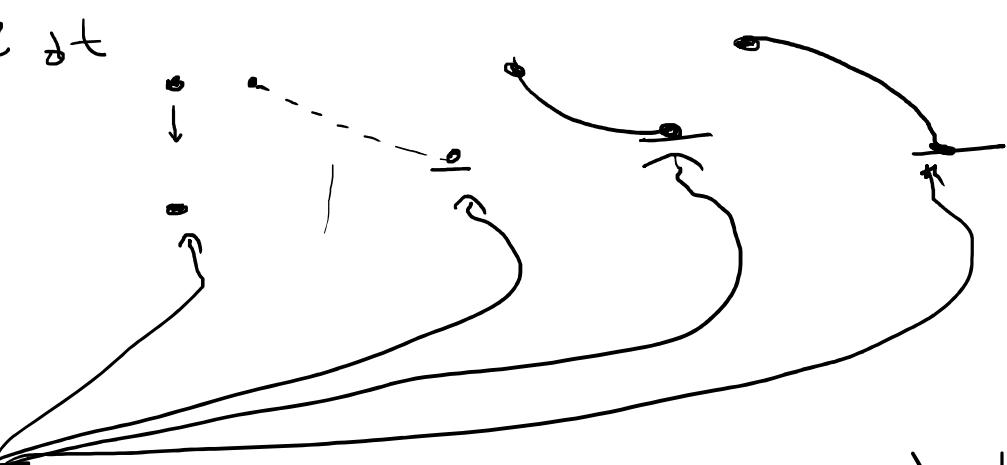
$$U_{g,1} + K_1 = U_{g,2} + K_2$$

$$mg h_1 + \frac{1}{2}mv_1^2 = mg h_2 + \frac{1}{2}mv_2^2$$

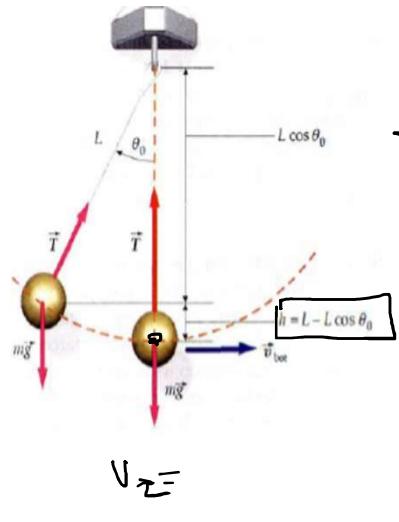
$$\cos \theta = \frac{L}{L+h}$$

$$(L+h) \cos \theta = L$$

$$gh_1 = \frac{1}{2}v_2^2 \Rightarrow \sqrt{2gh_1} = v_2$$



F_c únicamente hace trabajo



$$U_2 = \sqrt{2gh}$$

$$(U_2 = \sqrt{2g(L - L \cos \theta)})$$

Cinemática
f F constante. $\rightarrow \text{mu a}$

$$T = ?$$

$$\sum F_{y2} = ma_y$$

$$v_{2z} =$$

$$T - mg = ma_y$$

$$U_2^2 - U_1^2 = 2 \Delta g a_y$$

$$\frac{U_2^2}{2 \Delta g} = a_y = \frac{2gL(1 - \cos \theta)}{2L}$$

$$a_y = g(1 - \cos \theta)$$

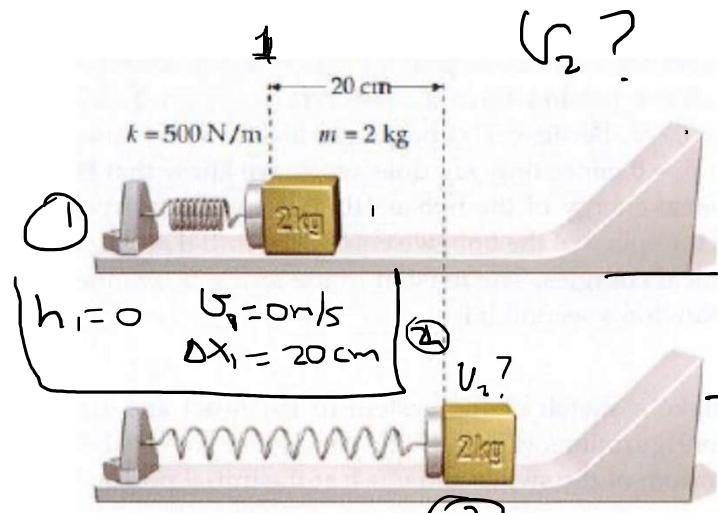
$$h = L(1 - \cos \theta)$$

$$T = m(a_y + g)$$

$$T = m(g(1 - \cos \theta) + g)$$

$$T = mg(1 - \cos \theta + 1)$$

$$T = mg(2 - \cos \theta)$$



$$\Delta E_{\text{me}} = 0$$

$$E_{\text{me},1} = E_{\text{me},2}$$



$$E_{\text{me},1} = E_{\text{me},3}$$

$$(E_{\text{me},2}) = E_{\text{me},3}$$

$$h_2 = 0$$

$$U_2 ?$$

$$h_2 = 0$$

$$\Delta x = 0$$

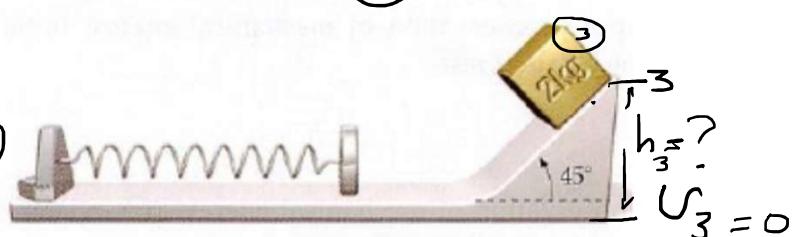
$$U_{R_1} + U_g + K_1 = U_{R_3} + K_3 + U_{g_3}$$

$$\frac{1}{2}k\Delta x_1^2 + mgh_1 + \frac{1}{2}m\dot{U}_1^2 = \frac{1}{2}k\Delta x_3^2 + mgh_3 + \frac{1}{2}m\dot{U}_3^2$$

$$\cancel{\frac{1}{2}k\Delta x_1^2} = \cancel{\frac{1}{2}m\dot{U}_1^2}$$

$$U_2 = \sqrt{\frac{k\Delta x_1^2}{m}} = \sqrt{\frac{500 \text{ N/m} \times (0.2 \text{ m})^2}{2 \text{ kg}}}$$

$$K_2 = \underline{\frac{1}{2}k\Delta x_2^2} = \underline{\frac{1}{2} \frac{500 \text{ N}}{\text{m}} \times (0.2 \text{ m})^2}$$



$$\Delta E_{\text{me}} = 0$$

$$E_{\text{me},2} = E_{\text{me},3}$$

$$K_2 + U_{g_2} = K_3 + U_{g_3}$$

$$\frac{1}{2}m\dot{U}_2^2 + mgh_2 = \frac{1}{2}m\dot{U}_3^2 + mgh_3$$

$$\cancel{\frac{1}{2}m\dot{U}_2^2} = \cancel{mgh_3}$$

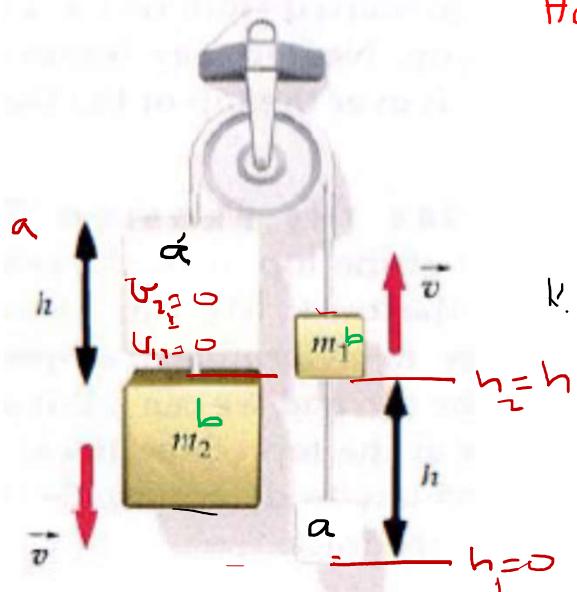
$$\dot{U}_2 = \sqrt{2gh_3}$$

$$K = mg h$$

$$h = \frac{K}{mg}$$

Hay Solamente una Fuerza Conservativa

F_G



$$\Delta E_{mec} = 0$$

$$E_{mec,1} = E_{mec,2}$$

$$K_1 + K_{1a} + K_{2a} + U_{g1a} + U_{g2a} = K_{1b} + K_{2b} + U_{g1b} + U_{g2b}$$

$$\frac{1}{2}m_1 U_{a_1}^2 + \frac{1}{2}m_2 U_{a_2}^2 + m_2 g h_{2a} + m_1 g h_{1a} =$$

$$\frac{1}{2}m_2 U_{2b}^2 + \frac{1}{2}m_1 U_{1b}^2 + m_2 g h_{b_2} + m_1 g h_{1b}$$

$$h_{2a} = h$$

$$U_{2b} = U_{1b}$$

$$h_{1b} = h$$

$$m_2 g h_{2a} = \frac{1}{2}m_2 U_{2b}^2 + \frac{1}{2}m_1 U_{1b}^2 = m_2 g h$$

$$m_2 g h = \frac{1}{2}m_2 U_{1b}^2 + \frac{1}{2}m_1 U_{1b}^2 = m_2 g h$$

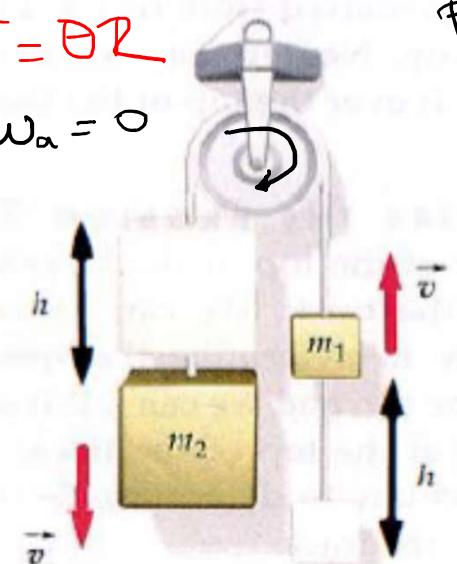
$$m_2 g h - m_2 g h = \frac{1}{2}U_{1b}^2 (m_1 + m_2)$$

$$\boxed{-\frac{2gh(m_2 - m_1)}{m_1 + m_2}} = U_{1b} - U_{2b}$$



$$\theta \\ S = \theta R$$

$$\omega_a = 0$$



Pulpa es un disco de radio R y masa M

$$\vec{\omega} = -\omega \hat{u}_z \quad I_o = \frac{1}{2} MR^2$$

$$K_{R_p} + K_1 + K_2 + U_{g1_a} + U_{g2_a} = K_{R_p} + K_{1_b} + K_{2_b} + U_{g1_b} + U_{g2_b}$$

$$\frac{1}{2}m_1 \dot{U}_{1_a}^2 + \frac{1}{2}m_2 \dot{U}_{2_a}^2 + \frac{1}{2}I\dot{\omega}^2 + m_1 g h_{1_a} + m_2 g h_{2_a} =$$

$$\frac{1}{2}m_1 \dot{U}_{1_b}^2 + \frac{1}{2}m_2 \dot{U}_{2_b}^2 + \frac{1}{2}I\dot{\omega}^2 + m_1 g h_{1_b} + m_2 g h_{2_b}$$

$$K_T = \text{Energía cinética}$$

Traslación

$$\boxed{\frac{1}{2}m\dot{U}^2} \rightarrow \frac{1}{2}I\dot{\omega}^2$$

K_R = Energía Rotacional.

Velocidad angular ω
masa \Rightarrow Momento de

$$\boxed{I}$$

$$\text{Inercia} \quad (\omega = \frac{U}{R})$$

$$\theta = R\omega$$

$$\frac{1}{2}U_b^2(m_1 + m_2) + \frac{1}{2}I\dot{\omega}_b^2 + m_1 gh = m_2 gh$$

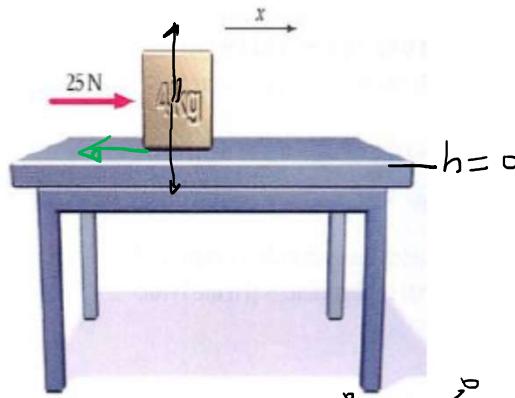
$$\cancel{\frac{1}{2}U_b^2} (m_1 + m_2) + \frac{1}{2}I \frac{U_b^2}{R^2} = m_2 gh - m_1 gh$$

$$\frac{1}{2}U_b^2 (m_1 + m_2) + \frac{1}{2}MR^2 \frac{U_b^2}{R^2} = gh (m_2 - m_1)$$

$$\frac{1}{2}U_b^2 (m_1 + m_2 + \frac{M}{2}) = gh (m_2 - m_1)$$

$$U_b = \sqrt{\frac{4gh(m_2 - m_1)}{(2m_1 + 2m_2 + M)}}$$

6. Usted empuja una caja de 4 kilogramos, que está al principio descansando sobre una mesa horizontal, con una fuerza horizontal de 25 N se desplaza una distancia de 3 m. El coeficiente de fricción cinética entre la caja y la mesa es 0.35. Encuentre al trabajo externo sobre el sistema de mesa de bloque, (b) la energía disipada por la fricción, (c) la energía cinética final de la caja, y d) la velocidad de la caja. Si Usted empuja una caja desde el reposo.



$$\Delta E_{mac} = k + \mu_2 \rightarrow \cancel{U_K}$$

$$\Delta E_{mac} = \Delta K$$

$$f_f = \mu N$$

$$f_f = \mu_k m g (-\vec{i})$$

$$\Delta x = \vec{d} \vec{i}$$

$$W_{ff} = -\Delta \mu_k m g$$

$$W_{F_{ext}} = \vec{F}_{ext} \cdot \vec{\Delta x} = 25 N \times 3 m (\vec{i}, \vec{i})$$

$$W_{ff} = -3 m \times 0.35 \times 4 kg \times 1.81 m/s^2 = -41.20 J$$

Energía disipada por fricción

$$F_{nc} = \frac{1}{2} F_f \rightarrow W_{nc} = W_{ff} + W_{F_{ext}}$$

$$W_{nc} = \Delta E_{mac} \quad K_f = \frac{1}{2} m v_f^2 \quad d = \Delta x = 3 m \vec{i}$$

$$\Rightarrow W_{nc} = K_f - K_i \quad K_i = \frac{1}{2} m v_i^2 = 0$$

$$W_{F_{ext}} = 25 N \times 3 m = 75 Nm$$

$$W_{nc} = W_{ff} + W_{F_{ext}} =$$

$$W_{nc} = -41.20 J + 75 J = K_f \Rightarrow$$

$$\frac{1}{2} m v_f^2 = W_{nc}$$

$$v_f^2 = 2 \frac{W_{nc}}{m}$$

$$v_f = \sqrt{\frac{2 \times 33.8 J}{4 kg}}$$

$$v_f = 4.11 m/s$$

$$F_{ext} = 25 N \vec{i}$$

$$m = 4 kg$$

$$\mu_k = 0.35$$

$$W_{F_{ext}} ?$$

$$\text{Energía disipada por fricción} = W_{ff}$$